

Atty. Docket No. 55123P226  
Express Mail Label No. EL802886430US

UNITED STATES PATENT APPLICATION

FOR

HIGH EFFICIENCY, LOW NOISE  
FREQUENCY TRIPLER AND METHOD

INVENTORS:

Robert S. Cargill  
Gary E. Mueller

PREPARED BY:

BLAKELY, SOKOLOFF, TAYLOR & ZAFMAN LLP  
12400 Wilshire Boulevard  
Seventh Floor  
Los Angeles, California 90025  
(714) 557-3800

20042655-010802

# HIGH EFFICIENCY, LOW NOISE FREQUENCY TRIPLER AND METHOD

## BACKGROUND OF THE INVENTION

### 1. Field of the Invention

5           The present invention relates to the field of frequency multipliers.

### 2. Prior Art

Existing frequency triplers are square wave generators that have filtered outputs to select the third harmonic in the square wave output. The circuit consists of an oscillator generating a frequency  $f$  and a modulator which, switched at  $f$ , produces a train of odd order harmonics in decreasing amplitude:

$$Z = K \times \text{SIGN}(\sin \omega t)$$

$$= K \times \frac{4}{\pi} \left( \sin \omega t + \frac{1}{3} \sin 3\omega t + \frac{1}{5} \sin 5\omega t + \dots \right)$$

where:       $\omega = 2\pi f$

This technique has the disadvantage that the desired harmonic is nearly 10dB below the fundamental signal, increasing the complexity of filtering required to select the third harmonic. Also, this approach results in extremely poor conversion efficiency, since over 90% of the signal power is wasted in undesired terms.

BRIEF SUMMARY OF THE INVENTION

High efficiency, low noise frequency tripler and method that generates an enhanced third harmonic of a frequency and suppresses the fundamental frequency component in the tripler  
5 output. The method comprises multiplying a constant plus a twice frequency component by a square wave at the fundamental frequency, such as by a modulator. The amplitude of the twice frequency component relative to the constant and the  
10 phase of the twice frequency component relative to the phase of the square wave are chosen to reduce the fundamental frequency component and enhance the third harmonic in the tripler output. An implementation using a differential Colpitts oscillator is disclosed.

1004655-010302

BRIEF DESCRIPTION OF THE DRAWINGS

Figure 1 is a block diagram of a VCO architecture that may be used to practice the present invention.

Figure 2 is a circuit diagram for a differential  
5 Colpitts oscillator based implementation of the present  
invention.

20250710 55123P226

DETAILED DESCRIPTION OF THE PREFERRED EMBODIMENT

The present invention provides a way to suppress the fundamental frequency component in a non-linear process used to generate the third and other odd harmonics of the fundamental frequency, improving conversion efficiency and reducing filtering requirements. Reduced broadband noise is another result of the improved conversion efficiency.

A preferred embodiment of the invention takes advantage of a VCO architecture that produces the fundamental frequency  $f$  as well as the second harmonic  $2f$ , depending upon where the output is taken. This is illustrated schematically in Figure 1, where the VCO generates the frequency components  $f$  and  $2f$ . The second harmonic, with an equal fixed component added (1 in the Figure), is applied to the analog port of a one-quadrant modulator MOD, with the fundamental frequency component providing the modulating signal. Thus:

$$Z = \text{SIGN}(\sin \omega t) \times \left( 1 + \sin \left[ 2\omega t + \frac{\pi}{2} \right] \right)$$

As shown in the above equation, the phasing is chosen such that a modulator transition occurs at every peak in the second harmonic signal. One effect is a slight increase in the RMS current in the  $2f$  multiplicand  $Y$  from the constant bias case. It also has the effect of raising the third

harmonic amplitude relative to the fundamental and broadband noise.

The effect can be seen by multiplying the analog multiplicand by the Fourier decomposition for the square

5 wave:

$$Z = (1 + \sin(2\omega t + \phi)) \times \frac{4}{\pi} \left( \sin \omega t + \frac{1}{3} \sin 3\omega t + \frac{1}{5} \sin 5\omega t + \dots \right)$$

Here, the only frequency components of substantial interest are the fundamental and the third harmonic. The resulting relationship, ignoring higher order products, is:

$$Z = \frac{4}{\pi} \left[ \left( \sin \omega t + \frac{1}{3} \sin 3\omega t \right) + \frac{1}{2} \left( \cos(\omega t + \phi) + \frac{1}{3} \cos(\omega t - \phi) - \cos(3\omega t + \phi) + \frac{1}{5} \cos(3\omega t - \phi) \right) \right]$$

Setting  $\phi = \frac{\pi}{2}$ , this becomes:

$$Z = \frac{8}{3\pi} \left[ \sin \omega t + \frac{7}{5} \sin 3\omega t \right]$$

15 Thus by selecting  $\phi = \frac{\pi}{2}$ , one may reduce the fundamental frequency component by 1/3 and simultaneously almost triple the third harmonic generation. All of this is achieved with only a slight increase in RMS current.

For a 22% increase in RMS current, third harmonic production is increased from  $\frac{4}{3\pi}$  to  $\frac{56}{15\pi}$ , or nearly 9dB.

Meanwhile, fundamental output is reduced from  $\frac{4}{\pi}$  to  $\frac{8}{3\pi}$ , or roughly 3.5dB. Thus conversion efficiency quadruples as the rejection of undesired terms improves by 12dB.

A circuit shown in Figure 2 employed to realize (approximate) these relationships in a preferred embodiment is built around a differential Colpitts oscillator. The Colpitts oscillator has the advantage of low noise and the differential nature provides 180° phase opposite output signals. The basic devices of the Colpitts oscillator are resistors R1 through R3, capacitors C1 through C6, inductors L1 and L2, and transistors Q1 through Q4. Note that the two transistors of a conventional differential Colpitts oscillator are split into four transistors, transistors Q1,Q2 and transistors Q3,Q4. Thus some of the core current from each half or leg of the differential oscillator devices is summed to provide a second harmonic signal approximating the  $1 + \sin\left(2\omega t + \frac{\pi}{2}\right)$  multiplicand described earlier. (Note that by way of example, a full wave rectified sine wave will provide a constant, a twice frequency component, and additional even harmonic components, the additional even harmonics having little effect on the performance of the

present invention. Other techniques may be used as desired

to generate a term in the general form of  $1 + a \sin\left(2\omega t + \frac{\pi}{2}\right)$

plus other even harmonics, where  $a$  is a constant.) The

remainder of the current is fed from the collectors of

5 transistors Q1 and Q4 into the differential load of inductors

L3 and L4. The inductive load serves to provide a voltage

with the appropriate phase shift to drive the modulator

(drive the bases of transistors Q5 and Q6). The modulator

uses the second harmonic common-mode signal described above

10 as the tail current for transistors Q5 and Q6. Specifically,

the inductors are used to provide the appropriate 90° phase

shift in the switching signal applied to the bases of

transistors Q5 and Q6 such that every transition of the

modulator occurs on the peak of the second harmonic. The

15 result is that the fundamental is multiplied by the second

harmonic substantially according to the equations calculated

above:

$$Z = \text{SIGN}(\sin \omega t) \times \left(1 + \sin\left(2\omega t + \frac{\pi}{2}\right)\right)$$

The tank circuits formed by capacitor C7, inductor L5

20 and resistor R4, and capacitor C8, inductor L6 and resistor

R5 provide resonant collector loads for transistors Q5 and

Q6, respectively, which are particularly responsive to the

third harmonic to provide the same as capacitively coupled to



the differential outputs outp and outn by coupling capacitors C9 and C10. The resistors R4 and R5 prevent excessive resonance in the tank circuits and broaden their response, as the present invention is intended to be used in an RF device  
5 wherein the Colpitts oscillator is tunable over a frequency range by varactors in the oscillator tank circuit (inductors L1 and L2 and capacitors C5 and C6).

While a preferred embodiment of the present invention has been disclosed herein, such disclosure is only for  
10 purposes of understanding the exemplary embodiments and not by way of limitation of the invention. It will be obvious to those skilled in the art that various changes in form and detail may be made in the invention without departing from the spirit and scope of the invention as set out in the full  
15 scope of the following claims.